

# **Quality Assurance and Global Optimization**

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**ARKI Consult and GAMS Development Corporation**

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# Introduction

- Background and Motivation
- Global Optimization with GAMS
  - Available solvers
  - Issues specific to global optimization codes
- Framework for reliability and performance testing
- Examples

# GAMS Overview

- Started as a Research Project at the World Bank 1976
- GAMS went commercial in 1987
- Opened European Office in Cologne, Germany 1996
- 10,000s of users in over 100 countries
- Unique position between the academic and commercial world

# Basic Principles

- Separation of model and solution methods
- Model types
  - LP, MIP, **NLP**, **MINLP**, MCP, MPEC
  - Stochastic Programming, MPSGE
- Multiple solvers
- Computing platform independence

# Supported Solvers

<a href="#"><u>BDMLP</u></a>	LP solver that comes with any GAMS system
<a href="#"><u>CONOPT</u></a>	Large scale NLP solver from ARKI Consulting and Development
<a href="#"><u>CPLEX</u></a>	High-performance LP/MIP solver from Ilog
<a href="#"><u>DECIS</u></a>	Large scale stochastic programming solver from Stanford University
<a href="#"><u>DICOPT</u></a>	Framework for solving MINLP models. Needs both an NLP solver and a MIP solver. From Carnegie M
<a href="#"><u>MILES</u></a>	MCP solver from University of Colorado at Boulder that comes with any GAMS system
<a href="#"><u>MINOS</u></a>	NLP solver from Stanford University
<a href="#"><u>MPSGE</u></a>	Modeling Environment for CGE models from University of Colorado at Boulder
<a href="#"><u>OSL</u></a>	High performance LP/MIP solver from IBM
<a href="#"><u>OSLSE</u></a>	OSL Stochastic Extension for solving stochastic models
<a href="#"><u>PATH</u></a>	Large scale MCP solver from University of Wisconsin at Madison
<a href="#"><u>SBB</u></a>	Branch-and-Bound algorithm from ARKI Consulting and Development for solving MINLP models, requi
<a href="#"><u>SNOPT</u></a>	Large scale SQP based NLP solver from Stanford University
<a href="#"><u>XA</u></a>	Large scale LP/MIP system from Sunset Software
<a href="#"><u>XPRESS</u></a>	High performance LP/MIP solver from Dash

# Beta Solvers

<b>BARON</b>	Branch-And-Reduce Optimization Navigator for proven global solutions from The Optimization Firm
<b>CONVERT</b>	Frame work for translating models into scalar models of other languages
<b>LGO</b>	Lipschitz global optimizer from Pinter Consulting Services
<b>MOSEK</b>	Large scale LP/MIP plus conic and convex non-linear programming system from EKA Consulting
<b>NLPEC</b>	MPEC to NLP translator that uses other GAMS NLP solvers
<b>OQMS</b>	Multi-start method for global optimization from Optimal Methods Inc.
<b>PATHNLP</b>	Large scale NLP solver for convex problems from University of Wisconsin at Madison

## Contributed Plug&Play Solvers

<a href="#"><u>AMPLwrap</u></a>	Framework for using AMPL solver for GAMS models
<a href="#"><u>DEA</u></a>	Large scale Data Envelop Analysis Solver from University of Wisconsin at Madison
<a href="#"><u>Kestrel</u></a>	Framework for using remote NEOS solvers with a local GAMS system
<a href="#"><u>QPwrap</u></a>	Quadratic programming in GAMS

# Supported Platforms

Solver/Platform availability - 20.7 June 14, 2002

	Intel		Sun Sparc	HP 9000	DEC Alpha	IBM RS-6000	SGI
	Windows 95/98/Me/NT/2000/XP	Linux	Solaris	HP-UX 10	Digital Unix 4.0	AIX 4.3	IRIX
BDMLP	✓	✓	✓	✓	✓	✓	✓
CONOPT	✓	✓	✓	✓	✓	✓	✓
CPLEX 7.5	✓	✓	✓	✓	✓	✓	✓
DECIS	✓	✓	✓		✓		✓
DICOPT	✓	✓	✓	✓	✓	✓	✓
MILES	✓	✓	✓	✓	✓	✓	✓
MINOS	✓	✓	✓	✓	✓	✓	✓
MPSGE	✓	✓	✓	✓	✓	✓	✓
OSL V3	✓	✓	✓	✓		✓	✓
PATH	✓	✓	✓	✓	✓	✓	✓
SBB	✓	✓	✓	✓	✓	✓	✓
SNOPT	✓	✓	✓	✓	✓	✓	✓
XA	✓	✓	✓	✓	✓	✓	
XPRESS 13.02	✓	✓	✓	13.01			

# GAMS/GLOBAL Solvers

The solvers differ in the methods they use, in whether they find globally optimal solution with proven optimality, and in the size of models they can handle, and in the format of models they accept.

- **BARON**. Branch-and-Reduce algorithm from N.Sahinidis, University of Illinois Urbana-Champaign
- **LGO**. Lipschitz Global Optimization from Pinter Consulting Services, Canada
- **OQMS**. OptQuest/NLP algorithms by OptTek Systems and Optimal Methods



# BARON

BARON is a computational system for solving non convex optimization problems to global optimality. Purely continuous, purely integer, and mixed-integer nonlinear problems can be solved with the software. The Branch And Reduce Optimization Navigator derives its name from its combining interval analysis and duality in its reduce arsenal with enhanced branch and bound concepts as it winds its way through the hills and valleys of complex optimization problems in search of global solutions.

# LGO

LGO combines rigorous statistical methods with traditional mathematical programming methods to find solutions within well defined bounds. Tailored versions of LGO have been applied successfully in number of large scale special purpose applications.

# OQMS

OQMS. This system combines existing the robust nonlinear optimization technologies with OptTek's state-of-the-art metaheuristic search procedures, including Tabu Search, Neural Networks, and Scatter Search, into a single composite method.

# Local Optimization Today

- Nonlinear modeling available in GAMS from the very beginning
- Variety of local solvers
  - NLP: MINOS, CONOPT, SNOPT, LSGRG, PATHNLP
  - MINLP: DICOPT, SBB

implementing different methods (SLP, SQP, GRG, B&B, outer approximation...) improve reliability of nonlinear modeling

- Initial point is crucial for success

# Global Codes and GAMS

- Global codes provide
  - Independence of starting point
  - Global/improved solutions
  - Bounds for solution quality
- (Almost) seamlessly exchange of local solvers with global solvers: `Option nlp=oqms;`
- Minimize risk of new technology for customers
  - Multiple Global Codes
  - Fallback to Local Solvers

# Open Issues for Global Codes

- Termination criteria
  - When to stop a multi-start method?
- Problem modification
  - Global solvers require bounding box
- Limited algebra
  - E.g. External functions (black box)
- Solution quality metrics

# Research v. Commercial Codes

- Run in “expert mode” tuned by the developer for a particular problem
- User wants to solve his business problem and wants to treat the solver as a black box
- Solver has to work decently in *all* cases
- Even if the algorithm fails, the solver has to be “*fail-safe*”

# QA Tests for Reducing Risk

- Replication of quality assurance results critical factor for establishing a new solver technology in the commercial world
- Non-reproducible tests damage the reputation of a solver
- Requirement: low cost replication of such results by an independent auditor



# Effective Testing

- Test cases
  - Widely available collection of standardized test instances
- Data collection tools
  - Automatic collection of solution and statistics
  - Capture test environment setting (hardware, software)
- Data analysis tools
  - Standard quality and performance measurements

# Test Cases

- Classification
  - Toy models
  - Academic Application Models
  - Commercial Application Models (difficult to collect)
- Growing GAMS Model Collections
  - GAMS Model library <http://www.gams.com/modlib/modlib.htm>, with about 250 models from over 18 application areas
  - GLOBALLib <http://www.gamsworld.org/global/globallib.htm>, with about 250 scalar NLP models
  - MINLPLib <http://www.gamsworld.org/minlp/minlplib.htm>, with about 180 scalar MINLP models
  - MPECLib <http://www.gamsworld.org/mpec/mpeclib.htm>, which produces over 10,000 NLP models

# GAMS World Home Page



## GAMS World

The Worlds  
GLOBAL  
MINLP  
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MPSGE  
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### Welcome to the GAMS World



This is the home page of the GAMS World, a web site aiming to bridge the gap between academia and industry by providing highly focused forums and dissemination services in specialized areas of mathematical programming.

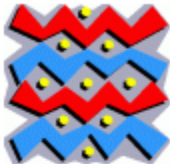
Substantial progress was made in the 1980s and 1990s with the development of algebra based modeling systems, algorithms, and computer codes to solve large and complex mathematical programs. The application of these tools, however, was less than expected. The abstraction, expression, and translation of real world problems into reliable and effective operational systems requires highly specialized and domains specific knowledge. The process of acquisition and dissemination of this knowledge is complex and poorly understood and the number of "good modelers" is much less than we all hoped for. Similarly, the process of transforming a new algorithm into a reliable and effective solution system is a slow and expensive process and there are few "good implementers". This web site hopes to address some of these problems by helping with the collection and dissemination of domain specific information and knowledge that is outside the established channels because of its content or form.

For example, model structures and results get published in commercial and academic papers but it is virtually impossible to reproduce any of those results or lift model components and data from one study to be used in some other study. Algorithm implementers face a similar dilemma when trying to get their hands on real world data models and data to test and refine their systems. This web site offers a few, well focused and maintained services to help with the dissemination of problems and solutions.

GAMS World is featured by [GAMS Development Corp.](#) and [GAMS Software GmbH](#)

# MINLP Lib

Address  <http://www.gamsworld.org/minlp/minplib/minlpstat.htm>  [Links >>](#)




[ [MINLP World Home](#) | [Board](#) | [Solvers](#) | [MINLPLib](#) | [Links](#) | [MINLP-List](#) | [Search](#) | [Contact](#) ]

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## MINLPLib Model Statistics

Name	#Eqs	#Vars	#DVars	#NZ	#NNZ	BestInt	at Point
<a href="#">4stufen</a>	99	150	48	319	87	116329.7000	<a href="#">p1</a>
<a href="#">alan</a>	8	9	4	24	3	2.9250	<a href="#">p1</a>
<a href="#">batch</a>	74	47	24	191	22	285506.5000	<a href="#">p1</a>
<a href="#">batchdes</a>	20	20	9	53	10	167427.7000	<a href="#">p1</a>
<a href="#">beuster</a>	115	158	52	398	159	116348.0000	<a href="#">p1</a>
<a href="#">cecil 13</a>	899	841	162	2812	360	-115570.3000	<a href="#">p1</a>
<a href="#">contvar</a>	285	297	87	1281	530	809149.8000	<a href="#">p1</a>
<a href="#">csched1</a>	23	77	63	174	8	-30639.2600	<a href="#">p1</a>
<a href="#">csched2</a>	138	401	308	958	58	-166102.0000	<a href="#">p1</a>
<a href="#">deb10</a>	130	183	11	692	432	209.4278	<a href="#">p1</a>
<a href="#">deb6</a>	508	476	20	2342	1432	201.7393	<a href="#">p1</a>
<a href="#">deb7</a>	898	814	10	4116	2816	116.5846	<a href="#">n1</a>

 Internet

Address  [http://www.gamsworld.org/global/globallib/ex7\\_3\\_6.htm](http://www.gamsworld.org/global/globallib/ex7_3_6.htm)  Go  Links >>



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**ex7\_3\_6.gms:**

**References:**

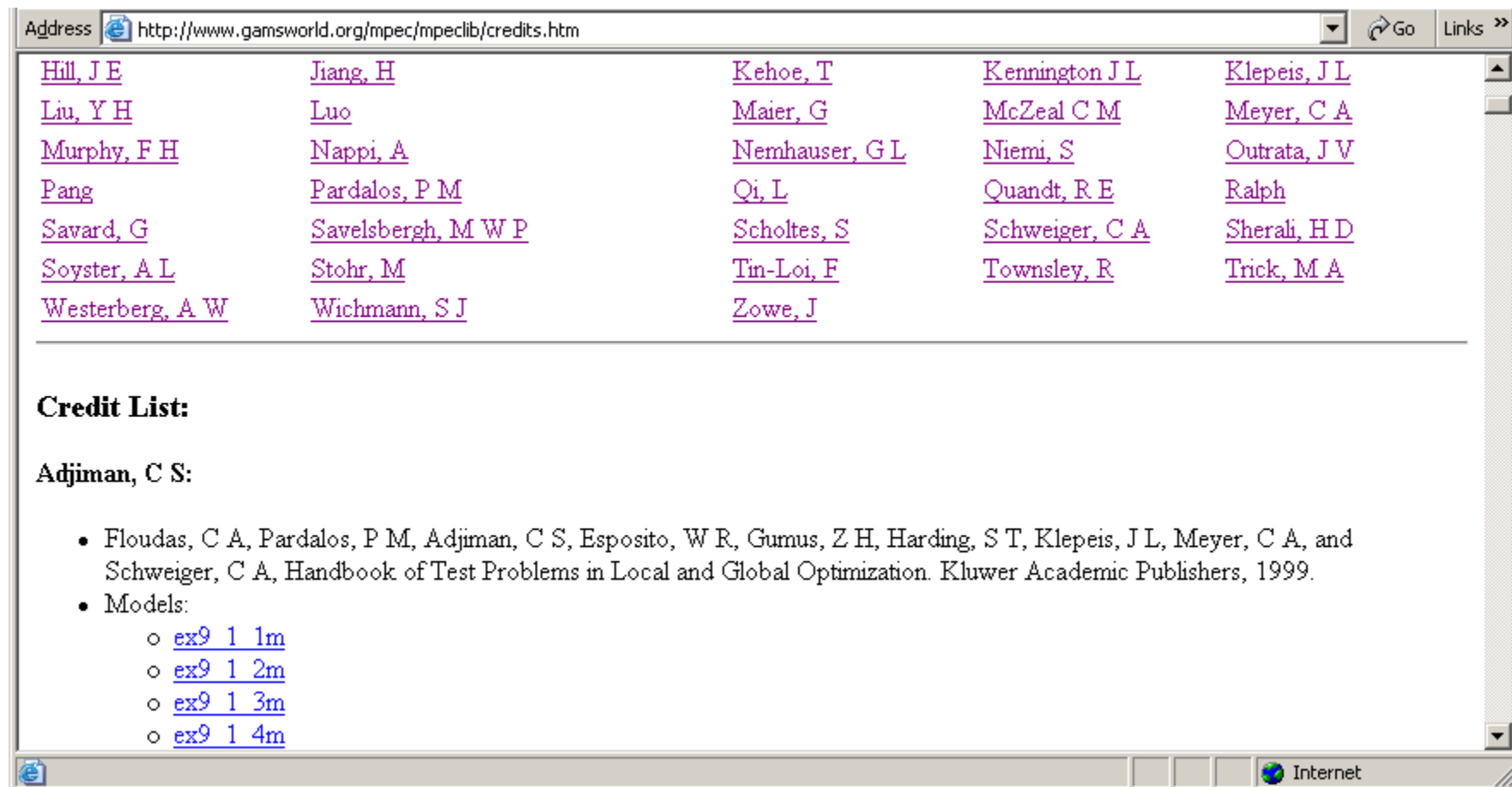
- Floudas, C A, Pardalos, P M, Adjiman, C S, Esposito, W R, Gumus, Z H, Harding, S T, Klepeis, J L, Meyer, C A, and Schweiger, C A, Handbook of Test Problems in Local and Global Optimization. Kluwer Academic Publishers, 1999.
- Barmish, B R, New Tools for Robustness of Linear Systems. MacMillan Publishing Company, New York, NY, 1994.
- Abate, M, Barmish, B, Murillo-Sanchez, C, and Tempo, R, Application of Some New Tools to Robust Stability Analysis of Spark Ignition Engines : A Case Study. IEEE Trans. Contr. Syst. Tech. 2 (1994), 22.
- Original source: Global Model of Chapter 7 [ex7.3.6.gms](#) from Floudas e.a. Test Problems

**Point:** [p1](#)

**Best known point:** [p1](#) with value 0.0000

  Internet

# MPEC Lib



Address <http://www.gamsworld.org/mpec/mpeclib/credits.htm> Go Links >>

<a href="#">Hill, J E</a>	<a href="#">Jiang, H</a>	<a href="#">Kehoe, T</a>	<a href="#">Kennington J L</a>	<a href="#">Klepeis, J L</a>
<a href="#">Liu, Y H</a>	<a href="#">Luo</a>	<a href="#">Maier, G</a>	<a href="#">McZeal C M</a>	<a href="#">Meyer, C A</a>
<a href="#">Murphy, F H</a>	<a href="#">Nappi, A</a>	<a href="#">Nemhauser, G L</a>	<a href="#">Niemi, S</a>	<a href="#">Outrata, J V</a>
<a href="#">Pang</a>	<a href="#">Pardalos, P M</a>	<a href="#">Qi, L</a>	<a href="#">Quandt, R E</a>	<a href="#">Ralph</a>
<a href="#">Savard, G</a>	<a href="#">Savelsbergh, M W P</a>	<a href="#">Scholtes, S</a>	<a href="#">Schweiger, C A</a>	<a href="#">Sherali, H D</a>
<a href="#">Soyster, A L</a>	<a href="#">Stohr, M</a>	<a href="#">Tin-Loi, F</a>	<a href="#">Townsend, R</a>	<a href="#">Trick, M A</a>
<a href="#">Westerberg, A W</a>	<a href="#">Wichmann, S J</a>	<a href="#">Zowe, J</a>		

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**Credit List:**

**Adjiman, C S:**

- Floudas, C A, Pardalos, P M, Adjiman, C S, Esposito, W R, Gumus, Z H, Harding, S T, Klepeis, J L, Meyer, C A, and Schweiger, C A, Handbook of Test Problems in Local and Global Optimization. Kluwer Academic Publishers, 1999.
- Models:
  - [ex9 1 1m](#)
  - [ex9 1 2m](#)
  - [ex9 1 3m](#)
  - [ex9 1 4m](#)

Internet

# Data Collection Tools

- Status/performance/exception information
- GAMS Trace facility automatically collects
  - Model statistics
  - Non-default input options
  - Solver and solution statistics
  - Execution environment information
    - Version control of solvers

# Data Analysis Tools

- Integral part of the quality assurance process at GAMS
- Processing of trace results
  - Build-in tools for status information
  - Custom GAMS programs
  - Performance World Tools
    - Performance measurements
    - Graphical/tabular representations



# Performance World



## Performance World

**Editorial Board**

**PerformanceLib**

**Performance Tools**

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### Welcome to the Performance World!

Performance World is a forum for discussion and dissemination of information and tools about all aspects of performance testing of mathematical programming problems. This world has been established in response to user demands for independent and reproducible performance results.

Overall performance highly depends on problem formulation, solver, and tuning parameters. Our performance tools are designed to serve the different needs of our user community. One user may be interested in finding the most reliable way to solve a proprietary or classified model. On the other hand, an academic researcher may be interested in testing a new algorithm against a set of existing test problems and competing approaches. The main features are:

- Uniform access to a comprehensive set of established and new test problems
- Automation tools for collecting performance measurements
- Tools for analyzing and visualizing test results

### What's New:

- Try our online [PAVER Server](#) for automated performance analysis and batch file creation
- New tools for [analyzing non-convex or discrete models](#)
- MINLP type models from the [MINLP World](#) have been added to the [PerformanceLib](#) A [tutorial](#) (August, 2002)

# Open Testing Architecture

- Test models
  - Open source GAMS models
  - Automatic translation into different formats, e.g. AMPL
  - Web/Email interface for this translation service
- Trace facility API
  - ASCII import/export of trace files
- Analysis tools
  - open source GAMS programs
  - Web interface for PAVER (**P**erformance **A**nalysis and **V**isualization for **E**ffortless **R**eproducibility)

# Translation Services



[ [GAMS World Home](#) | [GMS2XX Translator](#) | [Search](#) | [Contact](#) ]

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## Instructions

In order to use the GMS2XX translation service which is based on the "solver" [GAMS/CONVERT](#) you have to attach your model to an email and send it to our translation server at [gms2xx@gamsworld.org](mailto:gms2xx@gamsworld.org). You specify the language in the subject line, for example

Subject: GAMS

At the moment we support the following *languages*:

- AMPL
- BARON
- CplexLP
- CplexMPS
- GAMS
- LGO
- LINGO
- MINOPT
- ALL (this creates scalar versions of all supported languages, listed above)

Set I Products /P1\*P2/  
J Cutting Patterns /C1\*C2/;

Parameter c(J) cost of raw material /C1 1, C2 1/  
cc(J) cost of change-over of knives /C1 0.1, C2 0.2/  
b(I) width of product roll-type I /P1 460, P2 570/  
nord(I) number of orders of product type I /P1 8, P2 7/  
Bmax width of raw paper roll /1900/  
Delta tolerance for width / 200/  
Nmax max number of products in cut / 5/  
bigM max number of repeats of any pattern / 15/;

Variable y(J) cutting pattern  
m(J) number of repeats of pattern j  
n(I,J) number of products I produced in cut J  
obj objective variable;

Binary Variable y; Integer Variable m, n;

Equation defobj, max\_width(J), min\_width(J), max\_n\_sum(J),  
min\_order(I), cut\_exist(J), no\_cut(J);

defobj.. sum(j, c[j]\*m[j] + cc[j]\*y[j]) =e= obj;  
max\_width(j).. sum(i, b[i]\*n[i,j]) =l= Bmax;  
min\_width(j).. sum(i, b[i]\*n[i,j]) + Delta =g= Bmax;  
max\_n\_sum(j).. sum(i, n[i,j]) =l= Nmax;  
min\_order(i).. sum(j, m[j]\*n[i,j]) =g= nord[i];  
cut\_exist(j).. y[j] =l= m[j];  
no\_cut(j).. m[j] =l= bigM\*y[j];

m.up[j] = bigM; n.up[i,j] = nmax;

model trimloss /all/;  
solve trimloss minimize obj using minlp;

```

* MINLP written by GAMS Convert
Variables
b1,b2,i3,i4,i5,i6,i7,i8,x9;
Binary Variables b1,b2;
Integer Variables i3,i4,i5,i6,i7,i8;
Equations
e1,e2,e3,e4,e5,e6,e7,e8,e9,e10,
    e11,e12,e13;

e1.. 0.1*b1 + 0.2*b2 + i3 + i4 - x9
=E= 0;
e2.. 460*i5 + 570*i7 =L= 1900;
e3.. 460*i6 + 570*i8 =L= 1900;
e4.. 460*i5 + 570*i7 =G= 1700;
e5.. 460*i6 + 570*i8 =G= 1700;
e6.. i5 + i7 =L= 5;
e7.. i6 + i8 =L= 5;
e8.. i3*i5 + i4*i6 =G= 8;
e9.. i3*i7 + i4*i8 =G= 7;
e10.. b1 - i3 =L= 0;
e11.. b2 - i4 =L= 0;
e12.. - 15*b1 + i3 =L= 0;
e13.. - 15*b2 + i4 =L= 0;

* set non default bounds
i3.up = 15; i4.up = 15; i5.up = 5;
i6.up = 5; i7.up = 5; i8.up = 5;

Model m / all /;
Solve m using MINLP minimizing x9;

```

```

# MINLP written by GAMS Convert
var b1 binary;
var b2 binary;
var i3 integer >= 0, <= 15;
var i4 integer >= 0, <= 15;
var i5 integer >= 0, <= 5;
var i6 integer >= 0, <= 5;
var i7 integer >= 0, <= 5;
var i8 integer >= 0, <= 5;

minimize obj:
    0.1*b1 + 0.2*b2 + i3 + i4;

subject to

e2: 460*i5 + 570*i7 <= 1900;
e3: 460*i6 + 570*i8 <= 1900;
e4: 460*i5 + 570*i7 >= 1700;
e5: 460*i6 + 570*i8 >= 1700;
e6: i5 + i7 <= 5;
e7: i6 + i8 <= 5;
e8: i3*i5 + i4*i6 >= 8;
e9: i3*i7 + i4*i8 >= 7;
e10: b1 - i3 <= 0;
e11: b2 - i4 <= 0;
e12: - 15*b1 + i3 <= 0;
e13: - 15*b2 + i4 <= 0;

```

# Trace Facility ASCII Interface

## Trace file parameters

The column headers for traceopt=3 are as follows:

1. filename: GAMS model filename
2. modeltype: LP, MIP, NLP, etc.
3. solvername:
4. NLP def: default NLP solver
5. MIP def: default MIP solver
6. juliantoday: start day/time of job
7. direction: 0=min, 1=max
8. equnum: total number of equations
9. varnum: total number of variables
10. dvarnum: number of discrete variables
11. nz: number of nonzeros
12. nlnz: number of nonlinear nonzeros
13. optfile: 1= optfile included
14. modelstatus:
15. solvestatus:
16. obj: value of objective function
17. objest: objective function estimate
18. res used: resource time used (sec)
19. iter used: number of solver iterations
20. dom used:
21. nodes used:
22. user1: user comment - preceded by a #

# Performance Tools

## Download Performance tools:

Download the Performance Tools and sample data.

- [Ptools.zip](#)

Includes the following tools:

- [pprocess.gms](#) - performs all performance tools on a given set of trace files and combines output in a summary HTML page.
- [pprofile.gms](#) - performance profile routine for solver comparisons
- [plotprof.gms](#) - performance profile plotting routine using Gnuplotxy (Windows only)
- [restime.gms](#) - Resource time comparison utility
- [schulz.gms](#) - termination routine to ensure solvers terminate at resource time limit
- [square.gms](#) - solver outcome comparison utility

Also includes the following sample data files, where solvers have been renamed to generic A, B, C to hide proprietary data:

# PAVER Web Submission



[ [Performance World Home](#) | [Board](#) | [Tools](#) | [PerformanceLib](#) | [Links](#) | [Performance-List](#) | [Search](#) | [Contact](#) ]

## PAVER - Performance Analysis Web Submission Tool

Email Address (required):

Submit trace file:

Rename solver:

Trace 1 (required)

Trace 2 (required)

Trace 3

Trace 4

Trace 5

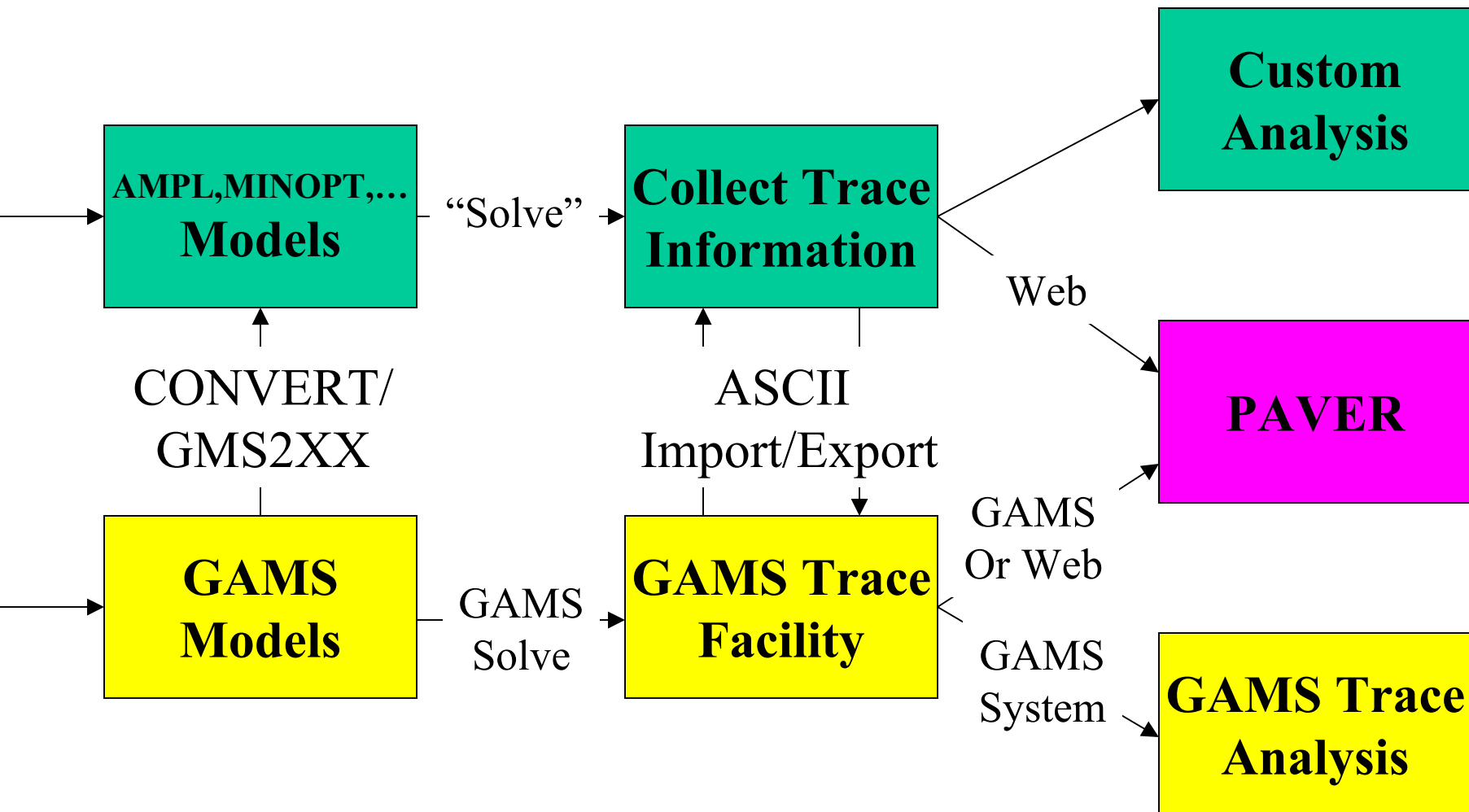
Trace 6

Trace 7

Trace 8



# Open Testing Architecture



# Example 1

- 24 MINLP Models from *Gupta, O K, and Ravindran, A, Branch and Bound Experiments in Convex Nonlinear Integer Programming. Management Science 13 (1985), 1533-1546.*
- Run all available GAMS MINLP solvers (*BARON, DICOPT, OQMS, SBB*) and *MINLP* (B&B based on *FILTER* by Fletcher and Leyffer) available through NEOS.
- Run all 24 models with all solvers (time limit 20 seconds) compare objective value with reference point.

MINLPlib Model Statistics - Microsoft Internet Explorer

File Edit View Favorites Tools Help

Back Forward Stop Home Search Favorites Media Print Mail

Address C:\gams\projects\mlib\scalar\MINLPSTAT.HTM Go Links

<a href="#">nvs01</a>	4	4	2	10	7	12.4697	<a href="#">p1</a>
<a href="#">nvs02</a>	4	9	5	20	16	5.9642	<a href="#">p1</a>
<a href="#">nvs03</a>	3	3	2	7	3	16.0000	<a href="#">p1</a>
<a href="#">nvs04</a>	1	3	2	3	2	0.7200	<a href="#">p1</a>
<a href="#">nvs05</a>	10	9	2	31	24	5.4709	<a href="#">p1</a>
<a href="#">nvs06</a>	1	2	0	2	0	1.2202	<a href="#">p1</a>
<a href="#">nvs07</a>							
<a href="#">nvs08</a>							
<a href="#">nvs09</a>							
<a href="#">nvs10</a>							
<a href="#">nvs11</a>							
<a href="#">nvs12</a>							
<a href="#">nvs13</a>							

## nvs12.gms:

### References:

- Tawarmalani, M, and Sahinidis, N V, Exact Algorithms for Global Optimization of Mixed-Integer Nonlinear Programs. In Pardalos, P M, and Romeijn, E, Eds, Handbook of Global Optimization - Volume 2: Heuristic Approaches. Kluwer Academic Publishers, 2001.
- Gupta, O K, and Ravindran, A, Branch and Bound Experiments in Convex Nonlinear Integer Programming. Management Science 13 (1985), 1533-1546.

**Point:** [p1](#)

**Best known point:** [p1](#) with value -481.2000

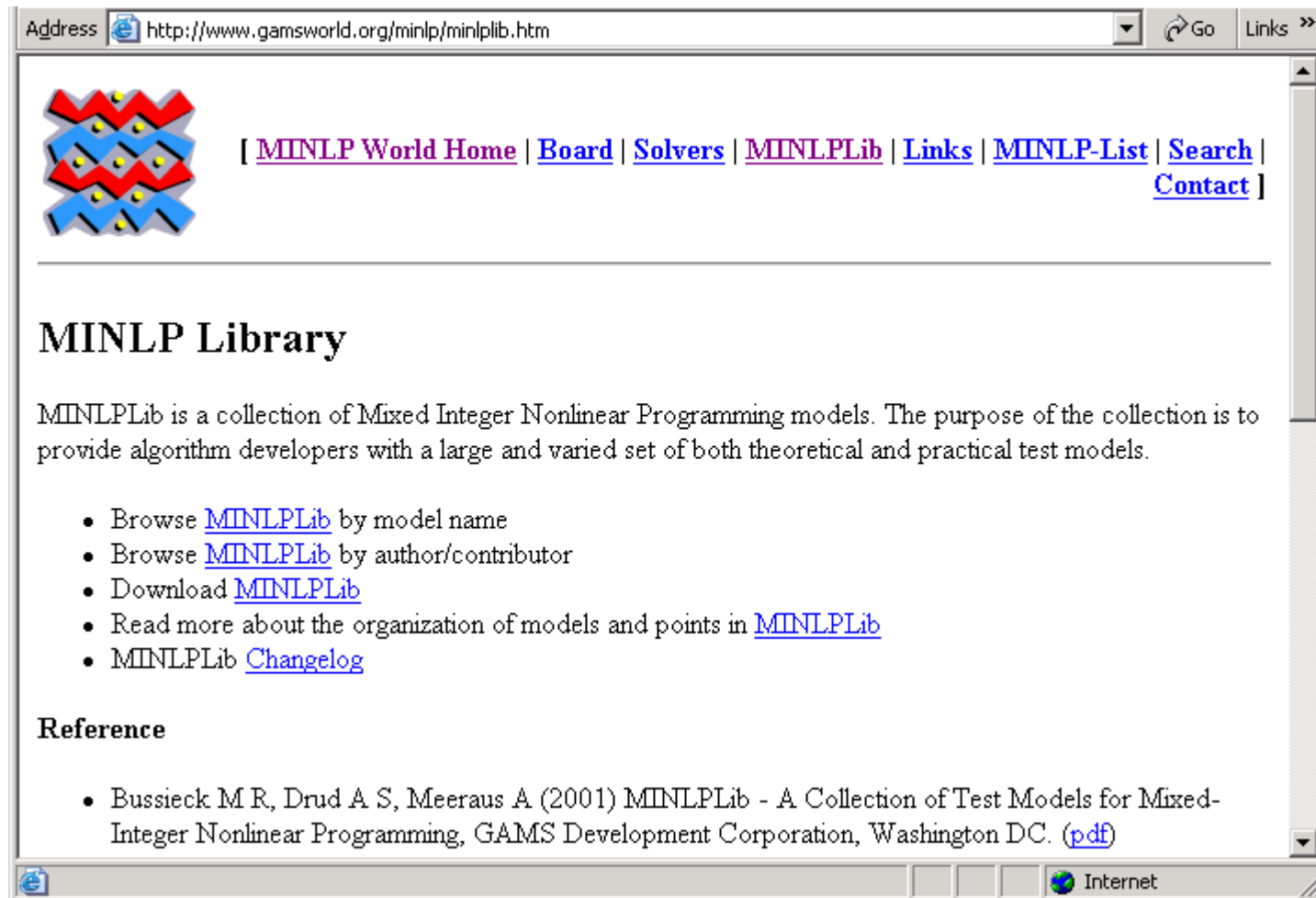
---




```


* MINLP written by GAMS Convert at 07/24/02 13:01:14
*
* Equation counts
*   Total      E        G        L        N        X        C
*     5         1         4         0         0         0         0
*
* Variable counts
*          x          b          i      s1s      s2s          sc          si
*   Total  cont  binary integer      sos1      sos2      scont      sint
*     5         1         0         4         0         0         0         0

```

# Download MINLPLib



Address  http://www.gamsworld.org/minlp/minplib.htm  Go  Links >>



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## MINLP Library

MINLPLib is a collection of Mixed Integer Nonlinear Programming models. The purpose of the collection is to provide algorithm developers with a large and varied set of both theoretical and practical test models.

- Browse [MINLPLib](#) by model name
- Browse [MINLPLib](#) by author/contributor
- Download [MINLPLib](#)
- Read more about the organization of models and points in [MINLPLib](#)
- MINLPLib [Changelog](#)

### Reference

- Bussieck M R, Drud A S, Meeraus A (2001) MINLPLib - A Collection of Test Models for Mixed-Integer Nonlinear Programming, GAMS Development Corporation, Washington DC. ([pdf](#))

    Internet

# Trace Data Generation for all GAMS Solvers

The screenshot shows the GAMS IDE interface with a window titled "gamside: C:\gams\tmp\nvs\nvs.gpr - [C:\gams\tmp\nvs\batch.gms]". The menu bar includes "File", "Edit", "Search", "Windows", and "Help". The toolbar contains icons for file operations and a search box. The active window is "batch.gms". The main text area contains the following code:

```

$eolcom //
$onecho > dorun.gms // Create batch script
set m / nvs01*nvs24 /
file fx / run.gms /; loop(m, put fx "$call gams " m.tl " pf=param" /);
$offecho
$call gams dorun.gms
$call gmsunzip -o -q minlplib nvs*.gms // Extract nvs problems from MINLPLib
$call rm -f baron.trc dicopt.trc oqms.trc sbb.trc // Clear the trace files

$echo reslim=20 traceopt=3 iterlim=1000000 lo=2 optcr=0 > param // Global options

$onecho > oqms.opt // Options to let OQMS terminate on time
iteration_limit 10000
max_solver_calls 10000
max_locals 10000
$offecho
$onecho > dicopt.opt // Option for convex problems
stop 1
optcr 0.0001
maxcycles 500
$offecho

$echo minlp=baron trace=baron.trc >> param
$include run
$echo minlp=dicopt mip=cplex nlp=conopt optfile 1 trace=dicopt.trc >> param
$include run
$echo minlp=oqms trace=oqms.trc optfile=1 >> param
$include run
$echo minlp=sbb nlp=conopt domlim=100 trace=sbb.trc >> param
$include run
$call cat oqms.trc baron.trc sbb.trc dicopt.trc > trace.trc

```

The status bar at the bottom shows "30: 107" and "Insert".

# AMPL Model Generation

IDE gamside: C:\gams\tmp\nvs\nvs.gpr - [C:\gam

IDE File Edit Search Windows Help

nv2ampl.gms batch.gms

```

$onecho > one.gms
$echo ampl %nvs%.mod > convert.c
$call gams %nvs% minlp convert c
$offecho

file fx / runall.gms /;
set m / nvs01*nvs24 /;
loop(m, put fx "$call gams one -
putclose fx;

execute "gams runall";

```

1: 1 Insert

Edit Mail Message -> gms2xx@gamsworld.org

Message Edit Search Utilities Spell Checker Privacy View Options

From: Franz Nelissen <FNe1issen@gams.com>  
 Reply-To: Franz Nelissen <FNe1issen@gams.com>  
 To: gms2xx@gamsworld.org  
 CC:  
 BCC:  
 Subject: ampl

nvs01.gms

The Bat!

From	To	Subject	Received	Created	Size
gms2xx@gam...	FNe1issen@g...	Your scalar AMPL model nvs01	11:59	11:59	2,645

From: gms2xx@gamsworld.org  
 To: FNe1issen@gams.com  
 Subject: Your scalar AMPL model nvs01

nvs01.zip

Dear GMS2XX user,

A zip file with your scalar model is attached. Please inspect memo.txt for warnings and translation incapacibilities.

Regards,

The GMS2XX Team

# AMPL Models

```

Emacs 20.7.1 c:/gams/tmp/nvs/nvs01.mod
Buffers Files Tools Edit Search Mule Help
MINLP written by GAMS Convert at 08/26/02
#
# Equation counts
#   Total      E      G      L
#   4          2      2      0
#
# Variable counts
#   Total      x      b      i      s1      s2
#   4          2      0      2      0      0
#
# FX          0      0      0      0
#
# Nonzero counts
#   Total      const      NL      DLL
#   10         3         7         0
#
# Reformulation has removed 1 variable and 1 equation

var i1 integer := 100, >= 0, <= 200;
var i2 integer := 100, >= 0, <= 200;
var x3 := 100, >= 0, <= 100;

minimize obj: 0.04712385*i2*(900 + i1^2)^0.5;

subject to

e1: 420.169404664517*sqrt(900 + i1^2) - x3
e2: - x3 >= -100;
e3: (2960.87631843 + 18505.4769901875*i2^2)^0.5

--\-- nvs01.mod (Text Fill)--L1--
End of buffer

Emacs 20.7.1 c:/gams/tmp/nvs/nvs02.mod
Buffers Files Tools Edit Search Mule Help
MINLP written by GAMS Convert at 08/26/02 18:06:51
#
# Equation counts
#   Total      E      G      L      N      X      C
#   4          4          0      0      0      0      0
#
# Variable counts
#   Total      x      b      i      s1s      s2s      sc      si
#   9          4      0      5      sos1      sos2      scont      sint
#   9          4      0      5      0          0          0          0
#
# FX          0      0      0      0      0      0      0      0
#
# Nonzero counts
#   Total      const      NL      DLL
#   20         4      16         0
#
# Reformulation has removed 1 variable and 1 equation

var i1 integer := 100, >= 0, <= 200;
var i2 integer := 100, >= 0, <= 200;
var i3 integer := 100, >= 0, <= 200;
var i4 integer := 100, >= 0, <= 200;
var i5 integer := 100, >= 0, <= 200;
var x6 >= 0, <= 92;
var x7 := 90, >= 90, <= 110;
var x8 := 20, >= 20, <= 25;

minimize obj: 9.999999999999999e-5*(5.3578547*i3^2 + 0.8356891*i1*i5 + 37.293239
*i1) + 5.9207859;

subject to

e1: - (0.0056858*i2*i5 + 0.0006262*i1*i4 - 0.0022053*i3*i5) + x6 = 85.334407;
e2: - (0.0071317*i2*i5 + 0.0029955*i1*i2 + 0.0021813*i3^2) + x7 = 80.51249;
e3: - (0.0047026*i3*i5 + 0.0012547*i1*i3 + 0.0019085*i3*i4) + x8 = 9.300961;

--\-- nvs02.mod (Text Fill)--L1--C0--A1-----

```



## WWW Interface

### MINLP (AMPL input)

The user must submit a model in [AMPL](#) format to solve a mixed integer nonlinearly constrained optimization problem. Examples of models in AMPL format can be found in the [MINLP - AMPL library](#).

The model is specified by a model file, and optionally, a data file and a commands file. If the command file is specified it must contain the AMPL solve command.

The commands file can contain any AMPL command or set [options for MINLP](#). Printing directed to standard out is returned to the user with the output.

Enter the AMPL model.

**AMPL model**(local file):

M: \nvs\nvs24.mod

Browse...





	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
1	*					date	direction	eqnum	varnum	dvarnum	nz	lnz	optfile	modelstat	solvesta	obj	object	res	iter	dom	nodes
2	NVS01		MINLPBB				0	4	4	2	10	7		8	1	12.4697		2.00E+01			
3	NVS02		MINLPBB				0	4	9	5	20	16		8	1	5.9642		2.00E+01			
4	NVS03		MINLPBB				0	3	3	2	7	3		8	4	16.0000		2.00E+01			
5	NVS04		MINLPBB				0	1	3	2	3	2		8	1	0.7200		2.00E+01			
6	NVS05		MINLPBB				0	10	9	2	31	24		8	1	5.4709		2.00E+01			
7	NVS06		MINLPBB				0	1	3	2	3	2		8	1	1.7703		2.00E+01			
8	NVS07		MINLPBB				0	3	4	3	9	3		8	1	4.0000		2.00E+01			
9	NVS08		MINLPBB				0	4	4	2	13	7		8	1	23.4497		2.00E+01			
10	NVS09		MINLPBB				0	1	11	10	11	10		8	1	-43.1343		2.00E+01			
11	NVS10		MINLPBB				0	3	3	2	7	6		8	1	-310.8000		2.00E+01			
12	NVS11		MINLPBB				0	4	4	3	13	12		8	1	-431.0000		2.00E+01			
13	NVS12		MINLPBB				0	5	5	4	21	20		8	1	-481.2000		2.00E+01			
14	NVS13		MINLPBB				0	6	6	5	31	30		8	1	-585.2000		2.00E+01			
15	NVS14		MINLPBB				0	4	9	5	20	16		8	1	-40358.1548		2.00E+01			
16	NVS15		MINLPBB				0	2	4	3	7	3		8	1	1.0000		2.00E+01			
17	NVS16		MINLPBB				0	1	3	2	3	2		8	1	0.7031		2.00E+01			
18	NVS17		MINLPBB				0	8	8	7	57	56		8	1	-1100.4000		2.00E+01			
19	NVS18		MINLPBB				0	7	7	6	43	42		8	1	-778.4000		2.00E+01			
20	NVS19		MINLPBB				0	9	9	8	73	72		8	1	-1098.4000		2.00E+01			
21	NVS20		MINLPBB				0	9	17	5	70	16		8	1	230.9222		2.00E+01			
22	NVS21		MINLPBB				0	3	4	2	8	7		8	1	-5.6848		2.00E+01			
23	NVS22		MINLPBB				0	10	9	4	31	24		8	1	6.0582		2.00E+01			
24	NVS23		MINLPBB				0	10	10	9	91	90		8	1	-1125.2000		2.00E+01			
25	NVS24		MINLPBB				0	11	11	10	111	110		8	1	-1033.2000		2.00E+01			
26																					

# Analysis Program

```

*=== Read in trace table
Table tracedata(*,*,col)
$ondelim
modelname,solvername,%col%
$offlisting
$call cat trace.trc minlpbb.csv | cut -d, -f1,3,6- > trace.tmp
$include trace.tmp
$onlisting
$offdelim
;

*=== Extract driving sets
Set modelname, solvername;
loop((u1,u2)$tracedata(u1,u2,'julian'),
  modelname(u1) = yes;
  solvername(u2) = yes;
);

parameter srep(u1,u2,col)
           mstat(u1,u2);

* Load Reference solution
$gdxin minlpstat
$load mstat

*=== Select columns
srep(modelname,solvername,c) = tracedata(modelname,solvername,c);
srep(modelname,'Reference','obj') = mstat(modelname,'BestInt');

Parameter gap;
gap(modelname,solvername,'agap') = round(srep(modelname,solvername,'obj') - srep(modelname,'Reference','obj'),3);
gap(modelname,solvername,'agap')$( srep(modelname,solvername,'modelstat') <> 1 and
  srep(modelname,solvername,'modelstat') <> 2 and
  srep(modelname,solvername,'modelstat') <> 8) = inf;
gap(modelname,solvername,'rgap') = gap(modelname,solvername,'agap')/abs(srep(modelname,'Reference','obj'));
gap(modelname,solvername,'obj') = srep(modelname,solvername,'obj');
gap(modelname,solvername,'cpu') = srep(modelname,solvername,'res');

display srep, gap;

```

# Results

```

----      167 PARAMETER gap

                obj                agap                rgap                cpu
NVS01.OQMS      15.806                3.336                0.268                2.218
NVS01.BARON     12.470                                0.110
NVS01.SBB       12.470                                0.410
NVS01.DICOPT    12.470                                0.035
NVS01.MINLPBB   12.470                                20.000
NVS02.OQMS       6.575                0.611                0.102                20.046
NVS02.BARON     5.964                                0.080
NVS02.SBB       5.964                                0.437
NVS02.DICOPT    5.964                                0.346
NVS02.MINLPBB   5.964                                20.000
NVS03.OQMS      16.000                                20.015
NVS03.BARON     16.000                                0.060
NVS03.SBB       16.000                                0.305
NVS03.DICOPT    16.000                                0.069
NVS03.MINLPBB   16.000                                20.000
NVS04.OQMS       0.720                                0.265
NVS04.BARON     0.720                                0.050
NVS04.SBB       0.720                                0.195
NVS04.DICOPT    2.120                1.400                1.944                0.227
NVS04.MINLPBB   0.720                                20.000

```

# Example 2

- 50 instances of NLP model LMP1 from *H. Konno and T. Kuno, “Linear multiplicative programming” Mathematical Programming, 56(51-64), 1992.*
- Run BARON in default mode and with 5 different option files (time limit 300 seconds).
- Compare Performance using PAVER.



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---

## Imp1.gms : Linear Multiplicative Model - Type 1

---

Generates and solves random linear multiplicative models of "Type 1." Problem instances are generated as proposed by Konno and Kuno. Model developed by N. Sahinidis.

---

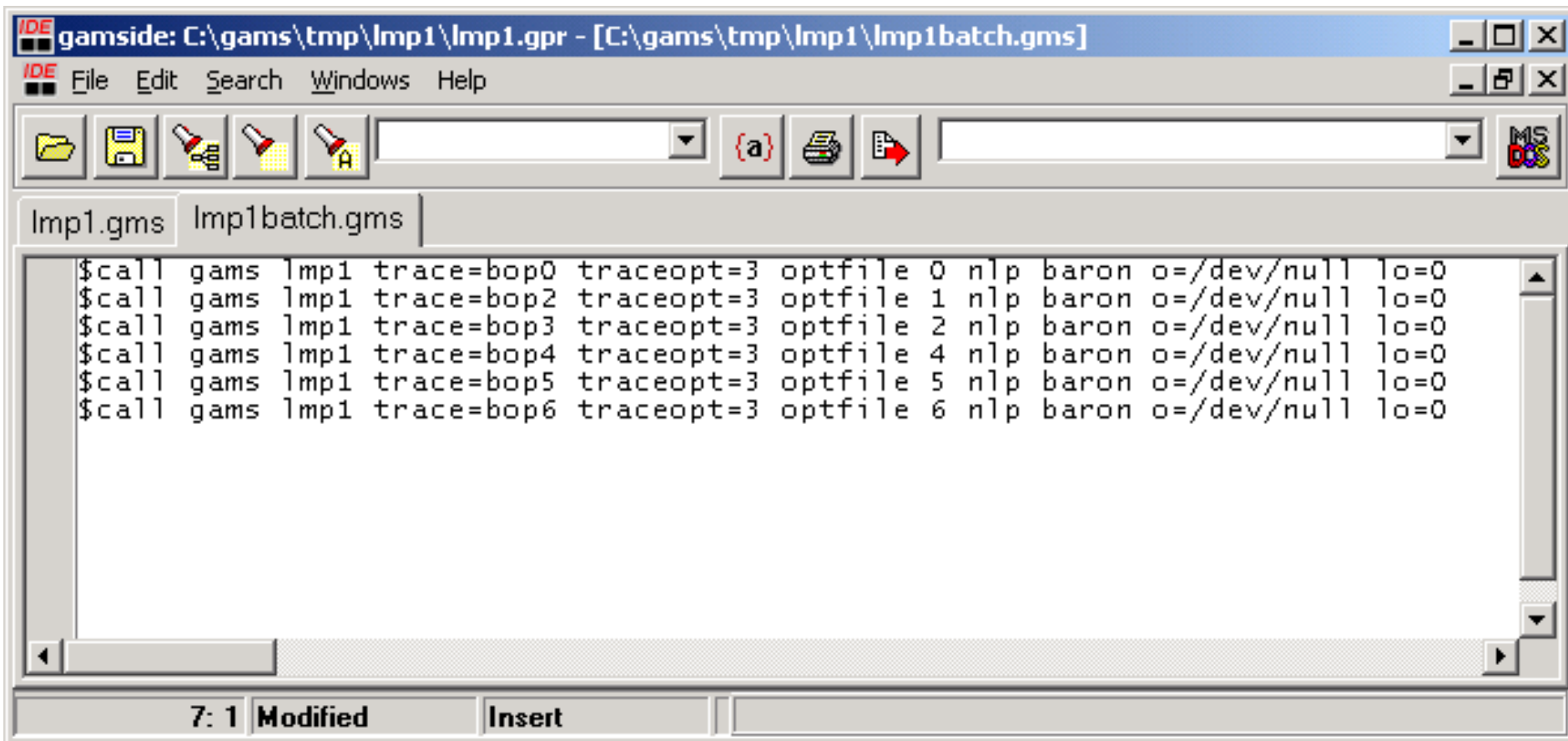
### References:

- Konno, H, and Kuno, T, Linear multiplicative programming. *Mathematical Programming* 56 (1992), 51-64.
  - Tawarmalani, M, and Sahinidis, N, *Convexification and Global Optimization in Continuous and Mixed-Integer Nonlinear Programming: Theory, Algorithms, Software, and Applications*. Kluwer, 2002.
- 

Large Model of Type: NLP

---

# LMP1 Trace Generation



The screenshot shows the GAMS IDE interface. The title bar reads "IDE gamside: C:\gams\tmp\lmp1\lmp1.gpr - [C:\gams\tmp\lmp1\lmp1batch.gms]". The menu bar includes "File", "Edit", "Search", "Windows", and "Help". The toolbar contains icons for file operations and a search icon. The active window is "lmp1batch.gms" and the text content is as follows:

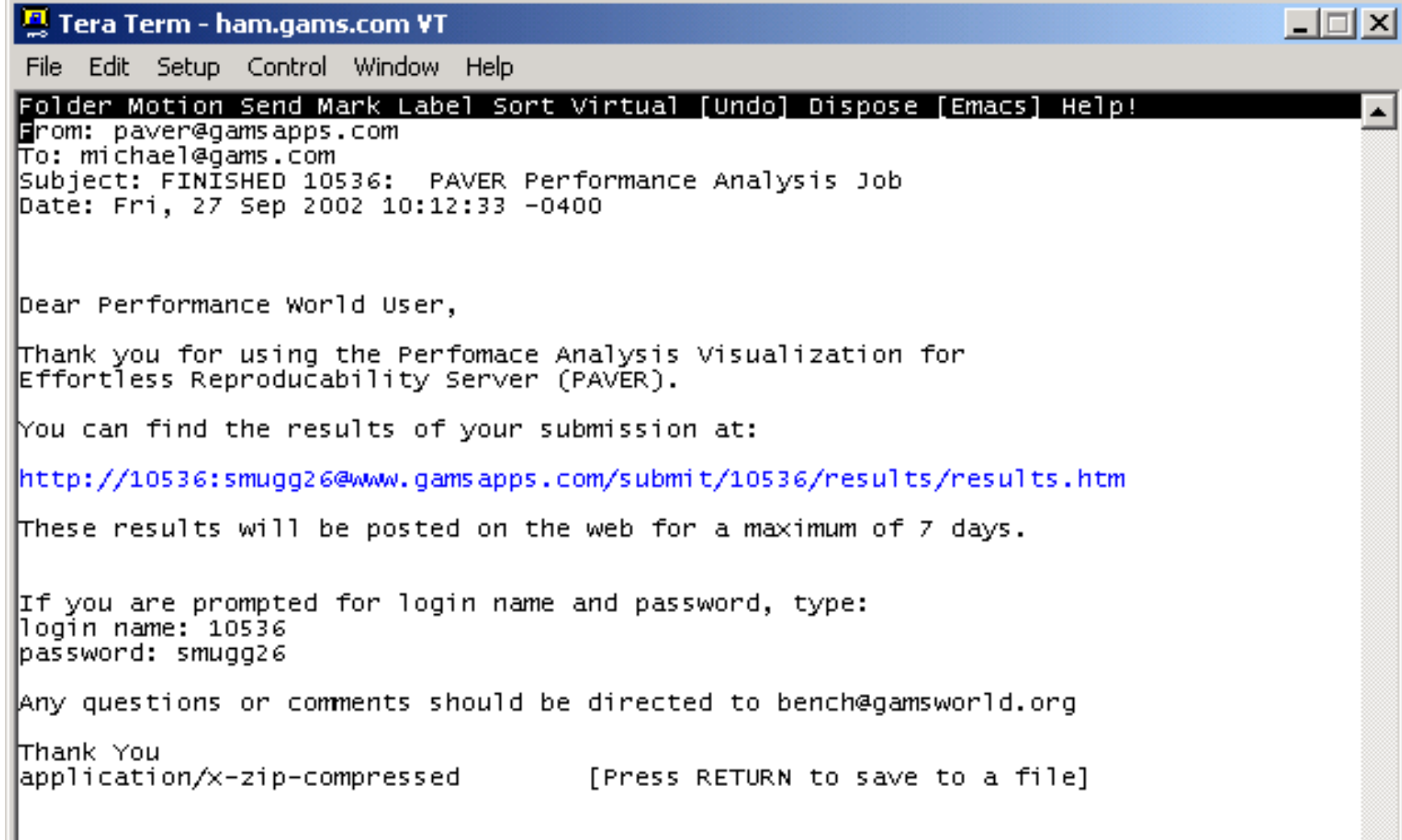
```
$call gams lmp1 trace=bop0 traceopt=3 optfile 0 nlp baron o=/dev/null lo=0
$call gams lmp1 trace=bop2 traceopt=3 optfile 1 nlp baron o=/dev/null lo=0
$call gams lmp1 trace=bop3 traceopt=3 optfile 2 nlp baron o=/dev/null lo=0
$call gams lmp1 trace=bop4 traceopt=3 optfile 4 nlp baron o=/dev/null lo=0
$call gams lmp1 trace=bop5 traceopt=3 optfile 5 nlp baron o=/dev/null lo=0
$call gams lmp1 trace=bop6 traceopt=3 optfile 6 nlp baron o=/dev/null lo=0
```

The status bar at the bottom indicates "7: 1 Modified" and "Insert" mode.





# PAVER Results by Email



```
Tera Term - ham.gams.com VT
File Edit Setup Control Window Help
Folder Motion Send Mark Label Sort Virtual [Undo] Dispose [Emacs] Help!
From: paver@gamsapps.com
To: michael@gams.com
Subject: FINISHED 10536: PAVER Performance Analysis Job
Date: Fri, 27 Sep 2002 10:12:33 -0400

Dear Performance World User,

Thank you for using the Performace Analysis Visualization for
Effortless Reproducibility Server (PAVER).

You can find the results of your submission at:
http://10536:smugg26@www.gamsapps.com/submit/10536/results/results.htm

These results will be posted on the web for a maximum of 7 days.

If you are prompted for login name and password, type:
login name: 10536
password: smugg26

Any questions or comments should be directed to bench@gamsworld.org

Thank You
application/x-zip-compressed          [Press RETURN to save to a file]
```

# Conclusions

- Framework for reliability and performance testing of (global) optimization codes.
- Open architecture for using this framework with models, modeling languages and solvers that are not necessarily connected with GAMS.
- Commitment to quality assurance in the optimization world (critical for success in the commercial environment).
- Presentation with all examples (will be) available at <http://www.gams.com/presentations>